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**Michael Goldberg\***, Department of Mathematical Sciences, University of Cincinnati, Cincinnati, OH 45221-0025, and **William Green**, Department of Mathematics, Rose-Hulman Institute of Technology, Terre Haute, IN 47803.  *$L^p$  Bounds for Wave Operators for the Schrödinger Equation with a Threshold Eigenvalue.*

The wave operators  $W_{\pm}$  are a valuable tool for linking properties of the Schrödinger evolution  $e^{itH}P_{ac}(H)$  to properties of the corresponding free evolution  $e^{-it\Delta}$ . We consider operators of the form  $H = -\Delta + V(x)$  in  $\mathbb{R}^n$ ,  $n \geq 5$  which have an eigenvalue at zero. The potential is assumed to decay at the rate  $|V(x)| \leq C(1 + |x|)^{-(n+3+\varepsilon)}$ .

It was recently proved by Yajima that the wave operators are bounded on  $L^p(\mathbb{R}^n)$  for all  $1 < p < \frac{n}{2}$ . We recover this result, including the  $p = 1$  endpoint, and show that the upper end of the range can be expanded if the eigenspace satisfies certain cancellation conditions: If  $\int V\phi dx = 0$  for each eigenfunction  $\phi$ , then  $L^p$ -boundedness of wave operators holds for  $1 \leq p < n$ . If the first moments of  $V\phi$  also vanish for each eigenfunction, then  $L^p$ -boundedness of wave operators holds for  $1 \leq p < \infty$ . (Received September 10, 2015)