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*Most trees are short and fat.*

Let  $T$  be any Galton-Watson tree. Write  $\text{vol}(T)$  for the volume of  $T$  (the number of nodes),  $\text{ht}(T)$  for the height of  $T$  (the greatest distance of any node from the root) and  $\text{wid}(T)$  for the width of  $T$  (the greatest number of nodes at any level). We study the relation between  $\text{vol}(T)$ ,  $\text{ht}(T)$  and  $\text{wid}(T)$ .

In the case when the offspring distribution  $p = (p_i, i \geq 0)$  has mean one and finite variance, both  $\text{ht}(T)$  and  $\text{wid}(T)$  are typically of order  $\text{vol}(T)^{1/2}$ , and have sub-Gaussian upper tails on this scale (A-B, Devroye and Janson, 2013). Heuristically, as the tail of the offspring distribution becomes heavier, the tree  $T$  becomes “shorter and bushier”. We prove a collection of theorems which can be viewed as justifying this heuristic. In particular, we show that the random variable  $\text{ht}(T)/\text{wid}(T)$  always has sub-exponential tails, and the random variable  $\text{ht}(T)/\text{vol}(T)^{1/2}$  always has sub-Gaussian tails.

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