

1116-VN-2660      **Shawn Michael Elledge\*** ([shawn.elledge@asu.edu](mailto:shawn.elledge@asu.edu)), Wanner Hall 301J, 6073 S. Backus Mall,  
Mail Code 2780, Mesa, AZ 85212-2780. *On Minimal Levels of Iwasawa Towers.*

In 1959, Iwasawa proved that the size of the  $p$ -part of the class groups of a  $\mathbb{Z}_p$ -extension grows as a power of  $p$  with exponent  $\mu p^m + \lambda m + \nu$  for  $m$  sufficiently large. Broadly, we explore algebraic conditions necessary for a given  $m$  to be sufficiently large.

More precisely, let  $CG_m^i$  (class group) be the  $\epsilon_i$ -eigenspace component of the  $p$ -Sylow subgroup of the class group of the field at the  $m$ -th level in a  $\mathbb{Z}_p$ -extension; and let  $IACG_m^i$  (Iwasawa analytic class group) be  $\mathbb{Z}_p[[T]]/((1+T)^{p^m} - 1, f(T, \omega^{1-i}))$ , where  $f$  is the associated Iwasawa power series. It is expected that  $CG_m^i$  and  $IACG_m^i$  be isomorphic; however, as of yet, this isomorphism is unestablished in general.

We consider the existence and the properties of an exact sequence

$$0 \rightarrow \ker \rightarrow CG_m^i \rightarrow IACG_m^i \rightarrow \text{coker} \rightarrow 0,$$

primarily focusing on verifying if  $m$  is sufficiently large that the kernel and cokernel of the above exact sequence have become well-behaved, providing similarity of growth both in the size and in the structure of  $CG_m^i$  and  $IACG_m^i$ . (Received September 22, 2015)