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*Compositions with Descents at Odd Plus Signs.*

For a positive integer  $n$ , a composition of  $n$  is an ordered summation  $x_1 + x_2 + \cdots + x_r$ , where  $1 \leq r \leq n$ , and  $x_1 + x_2 + \cdots + x_n = n$ . In general there are  $2^{n-1}$  such compositions for  $n$ . We want to consider those compositions of  $n$  where  $x_{2i-1} > x_{2i}$  for  $i \geq 1$ . For example, for  $n = 9$ , of the 256 compositions of 9, only 34 satisfy this condition. Three such compositions are  $3 + 2 + 2 + 1 + 1$ ,  $3 + 1 + 2 + 1 + 2$ , and  $4 + 3 + 2$ . In general the number of such compositions is  $F_n$ , the  $n^{\text{th}}$  Fibonacci number.

For a given  $n$ , results derived for these compositions include:

- (1) the total number of summands that occur;
- (2) the number of summands in even and odd positions;
- (3) the sums of all first, second, third, and fourth summands;
- (4) the number of compositions with three and four summands; and,
- (5) the number of times 1 occurs as a summand. (Received August 21, 2015)