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**Eva Czabarka** and **Laszlo A. Szekely\*** (szekely@math.sc.edu), szekely@math.sc.edu, and **Zoltan Toroczkai** and **Shanise Walker**. *Algebraic Monte-Carlo algorithms for the bipartite Partition Adjacency Matrix existence and construction problems*. Preliminary report.

Given a set  $W$  and numbers  $d(w)$  associated with  $w \in W$ , and a  $W_i : i \in I$  partition of  $W$ , with numbers  $c(W_i, W_j)$  associated with unordered pairs of partition classes, the Partition Adjacency Matrix *existence problem* asks whether there is a simple graph  $G$  on the vertex set  $W$  with degrees  $d_G(w) = d(w)$  for  $w \in W$ , with exactly  $c(W_i, W_j)$  edges with endpoints in  $W_i$  and  $W_j$ ; and the Partition Adjacency Matrix *construction problem* asks for such a graph, if they exist. (These problems are motivated by the concept of *assortativity* of network science, and the problems are conjectured to be NP-hard.) The *bipartite* version of these problems are more restricted:  $I = I_1 \cup I_2$  and  $c(W_i, W_j) = 0$  whenever  $i, j \in I_1$  or  $i, j \in I_2$ .

We provide algebraic Monte-Carlo algorithms for the bipartite Partition Adjacency Matrix existence and construction problems, which run in polynomial time, say, when  $|I|$  is fixed. When the algorithms provide a positive answer, they are always correct, and when the truth is positive, the algorithms fail to report it with small probability. (Received July 02, 2017)