

1135-05-936

**Alexander Diaz-Lopez\*** (diazlopezalexander@gmail.com), 800 Lancaster Ave (SAC 305), Department of Mathematics, Villanova University, Villanova, PA 19085, and **Pamela Harris**, **Erik Insko** and **Mohamed Omar**. *A proof of the peak polynomial positivity conjecture.*

We say that a permutation  $\pi = \pi_1\pi_2\cdots\pi_n \in \mathfrak{S}_n$  has a peak at index  $i$  if  $\pi_{i-1} < \pi_i > \pi_{i+1}$ . Let  $\mathcal{P}(\pi)$  denote the set of indices where  $\pi$  has a peak. Given a set  $S$  of positive integers, we define  $\mathcal{P}(S; n) = \{\pi \in \mathfrak{S}_n : \mathcal{P}(\pi) = S\}$ . In 2013 Billey, Burdzy, and Sagan showed that for subsets of positive integers  $S$  and sufficiently large  $n$ ,  $|\mathcal{P}(S; n)| = p_S(n)2^{n-|S|-1}$  where  $p_S(x)$  is a polynomial depending on  $S$ . They gave a recursive formula for  $p_S(x)$  involving an alternating sum, and they conjectured that the coefficients of  $p_S(x)$  expanded in a binomial coefficient basis centered at  $\max(S)$  are all nonnegative. In this talk we introduce a new recursive formula for  $|\mathcal{P}(S; n)|$  without alternating sums and we use this recursion to prove that their conjecture is true. (Received September 17, 2017)