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97370. *On Small Heights of Abelian Totally  $p$ -adic Numbers.*

The height of an algebraic number  $\alpha$  is a measure of how arithmetically complicated  $\alpha$  is. We say an algebraic number is totally real (or totally  $p$ -adic) if its minimal polynomial splits completely over  $\mathbb{R}$  (or  $\mathbb{Q}_p$ ). Further,  $\alpha$  is abelian if  $\mathbb{Q}(\alpha)$  is Galois with abelian Galois group over  $\mathbb{Q}$ . Let  $d \geq 2$  and  $p$  be a prime. Then there exists a smallest nontrivial height of an abelian totally  $p$ -adic algebraic number of degree  $d$ , which we will call  $\tau_{d,p}^{ab}$ . This talk will include the results describing aspects of the set  $\{\tau_{d,p}^{ab} : p \text{ is a prime}\}$ , and why it can be determined by a congruence condition on  $p$ . (Received September 12, 2017)