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**Jianzhen Liu\*** (jz10073@auburn.edu), 221 Parker Hall, Auburn University, Auburn, AL 36849,  
and **Tin-Yau Tam**, 221 Parker Hall, Auburn University, Auburn, AL 36849. *The general  $\phi$ -Hermitian solution to mixed pairs of quaternion matrix Sylvester equations.*

Let  $\mathbb{H}^{m \times n}$  be the space of  $m \times n$  matrices over  $\mathbb{H}$ , where  $\mathbb{H}$  is the real quaternion algebra. Let  $A_\phi$  be the  $n \times m$  matrix obtained by applying  $\phi$  entrywise to the transposed matrix  $A^T$ , where  $A \in \mathbb{H}^{m \times n}$  and  $\phi$  is a nonstandard involution of  $\mathbb{H}$ . We first give some properties of the Moore-Penrose inverse of the quaternion matrix  $A_\phi$ . Then we consider two systems of mixed pairs of quaternion matrix Sylvester equations  $A_1X - YB_1 = C_1$ ,  $A_2Z - YB_2 = C_2$  and  $A_1X - YB_1 = C_1$ ,  $A_2Y - ZB_2 = C_2$ , where  $Z$  is conditions for the existence of a solution  $(X, Y, Z)$  to those systems in terms of the ranks and Moore-Penrose inverses of the given coefficient matrices will be presented. Moreover, the general solutions to these systems are explicitly given when they are solvable. (Received September 26, 2017)