

1135-20-332

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Groups with the weak maximal condition on non-permutable subgroups.

Let H be a subgroup of a group G . Then H said to be *permutable* if it permutes with every subgroup of G , that is, $HK = KH$ for every subgroup K of G . Let \mathcal{P} be a subgroup theoretical property or class of groups, then $\bar{\mathcal{P}}$ is the class of all groups that either are not- \mathcal{P} groups or are trivial. A group G is said to satisfy the *weak maximal condition on \mathcal{P} -subgroups* (denoted by $\text{max-}\infty\text{-}\mathcal{P}$) if for every ascending chain $H_1 < H_2 < H_3 < \cdots < H_n < \cdots$ of \mathcal{P} subgroups of G , $|H_{i+1} : H_i|$ is infinite for only finitely many i . Thus, for example, on letting \mathcal{P} denotes the class of permutable subgroups, we may speak of groups satisfy $\text{max-}\infty\text{-}\bar{\mathcal{P}}$, the weak maximal condition on non-permutable subgroups. Groups with this property are the subject of our interest. The main result is; Let G be a group with the weak maximal condition on non-permutable subgroups. We prove that if G is a generalized radical group then G is either quasihamiltonian or a soluble-by-finite minimax group. (Received August 24, 2017)