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Alan Krinik*, ackrinik@cpp.edu, and **Uyen Nguyen, Ali Oudich, Pedram Ostadhassanpanjehali, Luis Cervantes, Chon In Luk, Matthew McDonough, Jeffrey Yeh and Lyheng Phey**. *Matrix properties of a class of birth-death chains and processes.*

Consider a birth-death chain on state space $S = \{0, 1, 2, \dots, H\}$ where $H \in \mathbb{N}$ with alternating birth probabilities $c_1, c_2, c_1, c_2 \dots$ and alternating death probabilities $a_1, a_2, a_1, a_2 \dots$ where $0 < c_i < 1$, $0 < a_i < 1$ and $a_i + c_i \leq 1$ for $i = 1, 2$. Assume $a_1 c_2 = a_2 c_1$ or $a_1 c_1 = a_2 c_2$. Suppose P is the one-step transition probability matrix associated with this birth-death chain and let P^* be the one-step transition probability matrix of the corresponding dual birth-death chain.

Conclusions:

- 1) The set of eigenvalues of P and P^* are the same and are determined as a function of H .
- 2) P^n and $(P^*)^n$ can be determined exactly for $n \in \mathbb{N}$.
- 3) Birth-death chains that have the same set of eigenvalues are identified.
- 4) Related results for birth-death processes and non-birth-death chains are discussed. (Received September 23, 2017)