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A rectilinear drawing of a graph  $G$  is an embedding of  $G$  into the plane such that the vertices of  $G$  are mapped to distinct points, and an edge connecting two vertices are mapped to the straight segment joining the corresponding points. In a rectilinear drawing, edges are allowed to cross, but an edge may not contain a vertex other than its endpoints. The rectilinear crossing number of  $G$ ,  $\overline{cr}(G)$ , is the smallest possible number of pairwise edge crossings in a rectilinear drawing of  $G$ . We investigate rectilinear crossing number of partite graphs. Namely, we discuss the following two problems.

The first problem is to establish the relationship between rectilinear crossing number and crossing number of 4-partite graphs. We show that there is a 4-partite graph, whose rectilinear crossing number and crossing number differ.

The second problem is Zarankiewicz's Conjecture for the complete bipartite graph  $K_{n,m}$  with  $n$  and  $m$  vertices in its partite vertex sets. We consider a special case of Zarankiewicz's Conjecture under the extra assumption that the partite vertex sets are separated by a straight line. We describe the current progress of proving Zarankiewicz's Conjecture in this case. (Received September 22, 2017)