

1135-VP-2660      **Eugene Han** (eugeneh@andrew.cmu.edu) and **David Offner\*** (offnerde@westminster.edu). *A new result on linear polychromatic colorings of the hypercube.*

Let  $Q_n$  denote the  $n$ -dimensional hypercube. For a fixed  $\ell \geq 1$ , a  $Q_\ell$ -coloring of  $Q_n$  is a coloring of the  $\ell$ -dimensional faces. A  $Q_\ell$ -coloring of  $Q_n$  is  $d$ -polychromatic if every  $Q_d$  in  $Q_n$  contains a  $Q_\ell$  of every color. For  $1 \leq \ell \leq d$ , let  $p^\ell(d)$  be the maximum number of colors such that any hypercube has a  $d$ -polychromatic  $Q_\ell$ -coloring with that number of colors. Polychromatic colorings of the hypercube were first studied by Alon, Krech, and Szabó. Their work, along with subsequent work of Offner established the value of  $p^1(d)$  for all  $d \geq 1$ . More recently, Chen introduced the notion of linear  $Q_\ell$ -colorings. We denote by  $p_{lin}^\ell(d)$  the maximum number of colors such that any hypercube has a  $d$ -polychromatic linear  $Q_\ell$ -coloring. Chen proved an upper bound on  $p_{lin}^2(d)$  for sufficiently large  $d$ . In this talk we will describe what is known about linear colorings and present a new theorem: For all  $d \geq 1$ ,  $p_{lin}^d(d+1) = 2$ . (Received September 26, 2017)