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For a ring  $R$ , Hilbert's Tenth Problem is the set  $HTP(R)$  of polynomial equations in several variables over  $R$  which have solutions in  $R$ . When we restrict our view to subrings  $R$  of  $\mathbb{Q}$ , we can therefore view  $HTP$  as an operator, mapping each subring (viewed as a subset of  $\mathbb{Q}$ ) to a subset of  $\mathbb{Z}[X_1, X_2, \dots]$ . As such,  $HTP$  satisfies Jockusch and Shore's definition of a *pseudajump operator*: by appropriate coding, we can consider it to map each subset of  $\mathbb{N}$  to another subset of  $\mathbb{N}$ , and the resulting set  $HTP(R)$  is uniformly computably enumerable in  $R$ , lying somewhere between  $R$  and its jump  $R'$  under Turing reducibility.

It is natural to ask whether this operator preserves Turing reducibility. We show that, unlike the true jump operator, it fails to do so: indeed, it can actually reverse Turing reductions. We also introduce a notion of completeness for sets under the  $HTP$ -operator, and show that, although very few sets are  $HTP$ -complete in this sense, every Turing degree contains an  $HTP$ -complete set. (Received September 17, 2018)