

1145-05-1202

**Danielle Wang\*** (diwang@mit.edu). *On roots of Wiener polynomials of trees.*

The *Wiener polynomial* of a connected graph  $G$  is the polynomial  $W(G; x) = \sum_{i=1}^{D(G)} d_i(G)x^i$  where  $D(G)$  is the diameter of  $G$ , and  $d_i(G)$  is the number of pairs of vertices at distance  $i$  from each other. We examine the roots of Wiener polynomials of trees. We prove that the collection of real Wiener roots of trees is dense in  $(-\infty, 0]$ , and the collection of complex Wiener roots of trees is dense in  $\mathbb{C}$ . We also prove that the maximum modulus among all Wiener roots of trees of order  $n \geq 31$  is between  $2n - 15$  and  $2n - 16$ , and we determine the unique tree that achieves the maximum for  $n \geq 31$ . Finally, we find trees of arbitrarily large diameter whose Wiener roots are all real. (Received September 20, 2018)