

1145-05-1561

Marisa Gaetz* (mgaetz@mit.edu). *Anti-power j -fixes of the Thue-Morse word.*

Recently, Fici, Restivo, Silva, and Zamboni introduced the notion of a k -anti-power, which is a word of the form $w^{(1)}w^{(2)} \cdots w^{(k)}$, where $w^{(1)}, w^{(2)}, \dots, w^{(k)}$ are distinct words of the same length. For an infinite word w and a positive integer k , define $AP_j(w, k)$ to be the set of integers m such that $w_{j+1}w_{j+2} \cdots w_{j+km}$ is a k -anti-power, where w_i denotes the i -th letter of w . Define also $\mathcal{F}_j(k) = (2\mathbb{Z}^+ - 1) \cap AP_j(\mathbf{t}, k)$, $\gamma_j(k) = \min(AP_j(\mathbf{t}, k))$, and $\Gamma_j(k) = \sup((2\mathbb{Z}^+ - 1) \setminus \mathcal{F}_j(k))$, where \mathbf{t} denotes the Thue-Morse word. In his 2018 paper, Defant shows that $\gamma_0(k)$ and $\Gamma_0(k)$ grow linearly in k . We generalize Defant's methods to prove that $\gamma_j(k)$ and $\Gamma_j(k)$ grow linearly in k for any nonnegative integer j . In particular, we show that $1/10 \leq \liminf_{k \rightarrow \infty} (\gamma_j(k)/k) \leq 9/10$ and $1/5 \leq \limsup_{k \rightarrow \infty} (\gamma_j(k)/k) \leq 3/2$. Additionally, we show that $\liminf_{k \rightarrow \infty} (\Gamma_j(k)/k) = 3/2$ and $\limsup_{k \rightarrow \infty} (\Gamma_j(k)/k) = 3$. (Received September 23, 2018)