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Lauren Rose* (rose@bard.edu), Bard College, Department of Mathematics, Campus Road PO Box 5000, Annandale on Hudson, NY 12504, and **Jeff Suzuki**. *Triangular Bases for Modules of Generalized Splines on Arbitrary Graphs*.

Let R be a commutative ring, and $G = (V, E, A)$ be an edge labeled graph with vertex set V , edge set E and edge weights A . A vertex labeling $(g_1, g_2, \dots, g_{|V|}) \in R^{|V|}$ is called a **generalized spline** if for any pair of vertices i, j joined by edge e with weight a , $g_i - g_j$ is an element of the ideal generated by a (equivalently, if R is the ring of integers, $g_i \equiv g_j \pmod{a}$). We designate the set of all such splines R_G .

In (2016), Gilbert, Tymoczko, and Viel asked for a characterization of R_G as an R module. We show that if R is a Euclidean domain, R_G is a free module with a triangular basis, and we provide an explicit construction for this basis. This generalizes work done by and with undergraduates at Smith College and Bard College. (Received September 24, 2018)