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Bethlehem, PA 18015. *Periodicity of Certain Generalized Continued Fractions.*

We have previously considered continued fractions with “numerator” a positive integer N , which we refer to as cf_N expansions. In particular, let E be a positive integer that is not a perfect square. For $N > 1$, \sqrt{E} has infinitely many cf_N expansions. There is a natural notion of the “best” cf_N expansion of \sqrt{E} . We have conjectured, based on extensive numerical evidence, that such a best expansion is not always periodic. From this evidence, it is difficult to predict for which N this expansion will be periodic. We show here that for any such E , there are infinitely many values of N for which this expansion is indeed periodic, more precisely, periodic of period 1 or 2, and we obtain formulas for a subset of these expansions in terms of solutions to Pell’s equation $x^2 - Ey^2 = 1$. (Received September 03, 2018)