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Robert Hines* (`robert.hines@colorado.edu`). *Badly approximable numbers over imaginary quadratic fields*. Preliminary report.

We recall the notion of nearest integer continued fractions over the Euclidean imaginary quadratic fields K and characterize the “badly approximable” numbers, (z such that there is a $C = C(z) > 0$ with $|z - p/q| \geq C/|q|^2$ for all $p/q \in K$), by boundedness of the partial quotients in the continued fraction expansion of z . Applying this algorithm to “tagged” indefinite integral binary Hermitian forms demonstrates the existence of entire circles in \mathbb{C} whose points are badly approximable over K , with effective constants.

By other methods (the Dani correspondence), we prove the existence of circles of badly approximable numbers over *any* imaginary quadratic field. Among these badly approximable numbers are algebraic numbers of every even degree over \mathbb{Q} , which we characterize. All of the examples we consider are associated with cocompact Fuchsian subgroups of the Bianchi groups $SL_2(\mathcal{O})$, where \mathcal{O} is the ring of integers in an imaginary quadratic field. (Received September 14, 2018)