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**Katherine Gallagher\*** (kgalla17@nd.edu), **Katja Vassilev** and **Lucia Li**. *Lacunarity of Han-Nekrasov-Okounkov  $q$ -series.*

A power series is called lacunary if “almost all” of its coefficients are zero. Integer partitions have motivated the classification of lacunary specializations of Han’s extension of the Nekrasov-Okounkov formula. More precisely, we consider the modular forms

$$F_{a,b,c}(z) := \frac{\eta(24az)^a \eta(24acz)^{b-a}}{\eta(24z)},$$

defined in terms of the Dedekind  $\eta$ -function, for integers  $a, c \geq 1$  where  $b \geq 1$  is odd throughout. Serre determined the lacunarity of the series when  $a = c = 1$ . Later, Clader, Kemper, and Wage extended this result by allowing  $a$  to be general, and completely classified the  $F_{a,b,1}(z)$  which are lacunary. Here, we consider all  $c$  and show that for  $a \in \{1, 2, 3\}$ , there are infinite families of lacunary series. However, for  $a \geq 4$ , we show that there are finitely many triples  $(a, b, c)$  such that  $F_{a,b,c}(z)$  is lacunary. In particular, if  $a \geq 4$ ,  $b \geq 7$ , and  $c \geq 2$ , then  $F_{a,b,c}(z)$  is not lacunary. Underlying this result is the proof the  $t$ -core partition conjecture proved by Granville and Ono. (Received September 17, 2018)