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Roger A Wiegand* (rwiegand1@unl.edu), Department of Mathematics, University of Nebraska, Lincoln, NE 68588-0130. *Semigroups of Modules*.

Let R be a commutative, Noetherian, local ring. We consider the semigroup of isomorphism classes of finitely generated R -modules, with the semigroup operation induced by the direct sum. This approach yields some “nice” properties that hold for all decompositions. For example, one *cannot* have indecomposable modules A and B such that $A \oplus A \oplus A \cong B \oplus B$. It also allows one to construct many “silly” examples. For instance, one can have four pairwise non-isomorphic indecomposable R -modules A, B, C, D such that $A \oplus B \oplus C \cong D^{(217)}$ (the direct sum of 217 copies of C).

In this talk I will describe how one obtains such silly examples and also consider the following question: Given a module M and a positive integer n , how many indecomposable modules occur as direct summands of $M^{(n)}$? This will lead to some open problems that are accessible to advanced undergraduates. (Received September 15, 2018)