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**Akeel Omairi\*** (aomairi2015@fau.edu), 6019 Boca Colony Dr. Apt 215, Boca Raton, FL 3443,  
and **Lee Klingler**. *Unique Decomposition of Direct Sums of Ideals*.

Let  $R$  be a commutative Noetherian ring. We say that  $R$  has the unique decomposition into ideals (UDI) property if each finite direct sum of ideals of  $R$  is uniquely decomposable as a direct sum of indecomposable  $R$ -ideal. For integral domain  $R$ , Goeters and Olbering showed that  $R$  has UDI if and only if  $R$  has at most one nonprincipal maximal ideal and has UDI locally at that nonprincipal maximal ideal (if it exists). For local domain  $R$ , they gave necessary and sufficient condition that  $R$  has UDI in terms of its integral closure. Their results were extended to reduced (commutative Noetherian) rings by Ay and Klingler. We show that if  $R$  is any commutative Noetherian ring, then  $R$  has UDI if and only if  $R$  has at most one nonprincipal maximal ideal and has UDI locally at that nonprincipal maximal ideal (if it exists). We also give an example of a ring without UDI but which has UDI modulo its nilradical, so that the UDI property does not lift modulo the nilradical. (Received September 16, 2018)