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**Michelle DeDeo\*** (mdedeo@unf.edu), 1 UNF Dr., Department of Mathematics and Statistics, Jacksonville, FL 32224. *The Heat Equation on the Poincare' Upper Half-Plane.*

Solving for the fundamental solution to the heat equation on a bounded domain is a classical problem in partial differential equations. When the domain is the circle, for instance, the fundamental solution of the heat equation can be described by a theta function. We talk about using a differential-difference operator  $\frac{\delta}{\delta t} - \Delta$  with  $\Delta$  the combinatorial Laplacian to model the heat equation on a finite graph analogue of Poincare's upper half-plane.

Finite analogues of the classical theta functions are shown to be solutions to the heat equation in this setting. The solutions involve zonal spherical functions which come with a natural periodicity. In addition, the related theta functions are automorphic forms. The resultant periodicity interweaves representation theory with the heat equation. (Received September 20, 2018)