

1145-49-2201

Nabin Kumar Sahu* (nabin6582@gmail.com). *A system of multivariate variational inequalities and the existence of its solutions in Banach spaces.*

In this paper we study a system of multivariate variational inequalities in a uniformly convex smooth Banach space by using the unique semi-inner product structure equipped in it. We consider the following problem:

Let X be a uniformly convex smooth Banach space with a unique semi-inner product $[\cdot, \cdot]$. Let K be a nonempty closed convex bounded subset of X . Let A_1, A_2, \dots, A_N be N -variables monotone demi-continuous mappings from K^N into X .

We discuss the existence solution of the following system of multivariate variational inequalities:

$$\begin{aligned} [A_1(x_1, x_2, \dots, x_N), y_1 - x_1] &\geq 0, \quad \forall y_1 \in K \\ [A_2(x_1, x_2, \dots, x_N), y_2 - x_2] &\geq 0, \quad \forall y_2 \in K \\ &\text{-----} \\ &\text{-----} \\ [A_N(x_1, x_2, \dots, x_N), y_N - x_N] &\geq 0, \quad \forall y_N \in K \end{aligned}$$

We also prove that the solutions set of the above system of multivariate variational inequalities is closed convex in K^N . Moreover we show that if A_1, A_2, \dots, A_N are strictly monotone, then the above system has a unique solution. (Received September 25, 2018)