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In this talk, we present recent results on the eigenvalues of the unique connected anti-regular graph  $A_n$ . Using Chebyshev polynomials of the second kind, we obtain a trigonometric equation whose roots are the eigenvalues and perform elementary analysis to obtain an almost complete characterization of the eigenvalues. In particular, we show that the interval  $\Omega = [-\frac{1-\sqrt{2}}{2}, \frac{-1+\sqrt{2}}{2}]$  contains only the trivial eigenvalues  $\lambda = -1$  or  $\lambda = 0$ , and any closed interval strictly larger than  $\Omega$  will contain eigenvalues of  $A_n$  for all  $n$  sufficiently large. We also obtain bounds for the maximum and minimum eigenvalues, and for all other eigenvalues we obtain interval bounds that improve as  $n$  increases. Moreover, our approach reveals a more complete picture of the bipartite character of the eigenvalues of  $A_n$ , namely, as  $n$  increases the eigenvalues are (approximately) symmetric about the number  $-\frac{1}{2}$ . We also obtain an asymptotic distribution of the eigenvalues as  $n \rightarrow \infty$ . Finally, the relationship between the eigenvalues of  $A_n$  and the eigenvalues of a general threshold graph is discussed. (Received July 30, 2018)