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Hong-Jian Lai, Mingquan Zhan and Taoye Zhang* (tuz3@psu.edu), Penn State Scranton,
120 Ridge View Dr, Dunmore, PA 18512, and **Ju Zhou.** *s-hamiltonian and s-hamiltonian
connected line graphs of claw-free graphs.*

For an integer $s \geq 0$, a graph G is s -hamiltonian if for any vertex subset $S \subseteq V(G)$ with $|S| \leq s$, $G - S$ is hamiltonian; and G is s -hamiltonian-connected if for any vertex subset $S \subseteq V(G)$ with $|S| \leq s$, $G - S$ is hamiltonian-connected. Thomassen in 1984 conjectured that every 4-connected line graph is hamiltonian. Lai and Shao [J. GraphTheory, 74 (2013), 344-358] proved that for a connected graph G and an integer $s \geq 5$, the line graph $L(G)$ is s -hamiltonian if and only if $L(G)$ is $(s + 2)$ -connected. The results presented in this talk are:

- (i). For an integer $s \geq 2$, the line graph $L(G)$ of a claw-free graph G is s -hamiltonian if and only if $L(G)$ is $(s + 2)$ -connected.
- (ii). The line graph $L(G)$ of a claw-free graph G is 1-hamiltonian-connected if and only if $L(G)$ is 4-connected. (Received September 21, 2018)