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**Borys Kadets\*** (bkadets@mit.edu). *Large arboreal Galois representations.*

Given a field  $K$ , a polynomial  $f \in K[x]$  of degree  $d$ , and a suitable element  $t \in K$ , the set of preimages of  $t$  under the iterates  $f^{\circ n}$  carries a natural structure of a complete rooted  $d$ -ary tree  $T_\infty$ . The Galois action on the roots of  $f^{\circ n}(x) - t$  gives rise to a homomorphism  $\phi : G_K \rightarrow \text{Aut}(T_\infty)$  known as the *arboreal Galois representation* attached to  $f$  and  $t$ . Arboreal representation is an arithmetic dynamics analogue of the Tate module. We study conditions under which the representation  $\phi$  is surjective. For  $d$  even we prove a criterion relating the surjectivity of  $\phi$  with the arithmetic of the critical orbit of  $f$ . When  $d \geq 20$  is even we use this criterion to exhibit examples of polynomials with maximal Galois action on the preimage tree, partially affirming a conjecture of Odoni (simultaneously and independently of our work two papers on Odoni's conjecture appeared; the full conjecture was proved by Joel Specter; Robert Benedetto and Jamie Juul proved the conjecture for most number fields). We also study the case of  $K = F(t)$  and  $f \in F[x]$  in which the corresponding Galois groups are the monodromy groups of ramified covers  $f^{\circ n} : \mathbb{P}_F^1 \rightarrow \mathbb{P}_F^1$ . (Received September 02, 2018)