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**J. W. Moon** and **Laura L.M. Yang\*** ([laura.yang@ucf.edu](mailto:laura.yang@ucf.edu)), Department of Mathematics, University of Central Florida, Orlando, FL 32816. *Asymptotic Results on Weighted Ordered Trees*. Preliminary report.

Binomial trees are defined as a sub-family of simply-generated trees, which have been studied by Meir and Moon and others. The paper is to investigate four statistics on simply-generated families: leaves, non-rightmost leaves, proper edges and proper vertices. We use Darboux's theorem to obtain asymptotic results on their expectations  $\mu_i(n)$  and variances, where  $n$  denotes the number of vertices in the trees being considered. For any constant  $0 < c < 1$  (for proper edges,  $0 \leq c \leq 1/2$ ), we prove that there exists a simply-generated family such that  $\mu_i(n)/n$  tends to  $c$  when  $n \rightarrow \infty$ . For binomial trees, we derive explicit expressions for  $\mu_i(n)$ . Using Lyapunov's condition, we prove the the distribution of the number of proper vertices is asymptotically normal. (Received September 16, 2019)