

1154-11-1941 **Sayok Chakravarty*** (s7chakra@ucsd.edu) and **Aitzin Cornejo-Reynoso**. *Extremal and Probabilistic Results for Sum-Difference Sidon Sets*.

Let $\mathcal{A} \subset [N]$. For $1 \leq i \leq n$, define

$$\sigma(i) := |\{(a, b) \in \mathcal{A}^2 : a \leq b, a + b = i\}|$$

and

$$\delta(i) := |\{(a, b) \in \mathcal{A}^2 : a \leq b, b - a = i\}|$$

\mathcal{A} is called Sidon if $\sigma(i) \leq 1$ for all i . We say a set \mathcal{A} is $\text{SD}_{2,g}$ if $\sigma(i) + \delta(i) \leq g$ for all i . In 1932 Hungarian mathematician Simon Sidon posed the following question: how dense can a $\text{SD}_{2,g}$ set be? We have shown if $\mathcal{A} \subset [N]$ is $\text{SD}_{2,g}$, then

$$|\mathcal{A}| \leq \sqrt{gN} + \left(\frac{1}{2}\sqrt{g} + \frac{1}{2}\right) \sqrt[4]{N} + 1$$

We also consider the related probabilistic problem for $\text{SD}_{2,2}$ sets. Let $A \subset [N]$ be a random subset in which each element of $[N]$ is chosen for membership in A with probability p . We find a threshold for a random set being $\text{SD}_{2,2}$ with probability that tends to 1/0 as $N \rightarrow \infty$.

We have found similar results for random sets $\mathcal{A} \subset [N]$ such that any $j \in [\frac{N}{2}, \frac{5N}{6}]$ can be represented as a sum and difference of two elements from \mathcal{A} in at least 1 way. (Received September 16, 2019)