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Xander Faber* (awfaber@super.org) and **Clayton Petsche**. *Totally T -adic functions of small height*. Preliminary report.

A nonzero algebraic number α is *totally p -adic* if its minimal polynomial (over \mathbb{Q}) splits completely over \mathbb{Q}_p . If α is not a $(p-1)$ st root of unity, then the naive logarithmic height of such an element is uniformly bounded away from zero by an equidistribution result of Bombieri/Zannier or an elementary inequality of Pottmeyer.

In this work, we introduce a geometric analogue. Fix a finite field \mathbb{F}_q , and consider the rational function field $\mathbb{F}_q(T)$. An algebraic function f that generates a separable extension of $\mathbb{F}_q(T)$ is *totally T -adic* if its minimal polynomial (over $\mathbb{F}_q(T)$) splits completely in the field of Laurent series $\mathbb{F}_q((T))$. We will discuss a lower bound for the height of any nonconstant totally T -adic function, and we will show that functions achieving the lower bound give rise to curious algebraic curves over \mathbb{F}_q with many rational points. We also investigate the limit-infimum of the heights of totally T -adic functions using a dynamical construction. (Received September 03, 2019)