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**Maria Fox** (mariafox@uoregon.edu), **Vlad Matei** (vmatei@uci.edu) and **Soumya Sankar\*** (ssankar3@wisc.edu). *Hecke Orbits and Unlikely Intersections*. Preliminary report.

Let  $X(1)$  denote the modular curve over the finite field  $\mathbb{F}_p$ . The Hecke orbit of a point  $(j(E_1), j(E_2) \cdots j(E_n)) \in X(1)^n(\overline{\mathbb{F}_p})$  is the set of  $(j(E'_1), \cdots j(E'_n)) \in X(1)^n(\overline{\mathbb{F}_p})$  such that  $E_i$  is isogenous to  $E'_i$  for each  $i$ . One can ask when a subvariety  $V$  of  $X(1)_{\mathbb{F}_p}^n$  satisfies the condition that  $V(\overline{\mathbb{F}_p})$  intersects *every* ordinary Hecke orbit. We provide a heuristic for the expected size of the intersection of  $V(\overline{\mathbb{F}_p})$  and a general ordinary Hecke orbit. (Received September 06, 2019)