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**Ningchuan Zhang\*** (nzhang28@illinois.edu). *Analogs of Dirichlet  $L$ -functions in  $K(1)$ -local homotopy theory.*

The relation between Eisenstein series and the  $J$ -homomorphism is an important topic in  $K(1)$ -local homotopy theory. Both sides are related to the special values of the Riemann  $\zeta$ -function. This relation is most clearly understood in the context of elliptic cohomology and topological modular forms.

Number theorists have studied the twistings of the Riemann  $\zeta$ -functions and Eisenstein series by Dirichlet characters. In this talk, we investigate the analogs of Dirichlet character twistings in homotopy theory. We will introduce the Dirichlet twists of the  $J$ -spectrum. The homotopy groups of these Dirichlet  $J$ -spectra are related to the special values of the Dirichlet  $L$ -functions, and thus to congruences of the twisted Eisenstein series. We will explain the connection between Dirichlet  $J$ -spectra and the twisted Eisenstein series by generalizing Katz's algebro-geometric explanation of congruences of the normalized Eisenstein series. (Received September 14, 2019)