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Simultaneous Decompression Based Cipher.

Let $|\mathbf{u}^1| = \delta_1$ and $|\mathbf{u}^2| = \delta_2$ where $\gcd(\delta_1, \delta_2) = 1$. The simultaneous decomposition of $(\mathbf{u}^1, \mathbf{u}^2)$ is defined as the set of binary vectors $\mathbf{v} \in \mathbf{V}$ satisfying $u_j^1 = \sum_{k=0}^{\delta_2-1} v_{k\delta_1+j}$ for each $j \in \mathbb{Z}_{\delta_1}$ and $u_j^2 = \sum_{k=0}^{\delta_1-1} v_{k\delta_2+j}$ for each $j \in \mathbb{Z}_{\delta_2}$. We exploit the isomorphism $\mathbb{Z}_{\delta_1\delta_2} \cong \mathbb{Z}_{\delta_1} \times \mathbb{Z}_{\delta_2}$ to formulate these constraints as a multi-dimensional Subset Sum problem with binary matrix solutions. The set of these matrices allows a graph representation, $\mathbb{G}_{\mathbf{V}}$, that is conjectured to contain a Hamiltonian cycle. It follows each \mathbf{v} may be uniquely represented by linearly-independent indices of $(\mathbf{u}^1, \mathbf{u}^2)$ and integer distance along this cycle. We construct a small example on $\delta_1\delta_2 = 21$ for demonstration, and discuss the pros and cons of this structure with respect to the principles of cryptography. (Received August 16, 2020)