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**Matthew C. Welsh\*** ([matthew.welsh@bristol.ac.uk](mailto:matthew.welsh@bristol.ac.uk)). *Bounds for theta sums.*

For a quadratic form  $Q$  in  $n$  variables and a real number  $M > 0$ , we consider the following theta sum,

$$\sum_{\mathbf{m} \in \mathbb{Z}^n} \chi\left(\frac{1}{M}\mathbf{m}\right) e^{2\pi i Q(\mathbf{m})},$$

where  $\chi$  is the indicator function of the unit cube  $(0, 1)^n$ . Cosentino and Flaminio (2015) have shown that for almost all  $Q$  this theta sum is  $\ll_Q M^{\frac{n}{2}} (\log M)^a$  for an explicit  $a > 0$  using properties of abelian actions on compact nilmanifolds. Here we present a new approach (joint with Jens Marklof, Soren Mikkelsen, and Gene Kopp) to producing bounds of the same form for almost all  $Q$  using theta functions defined via the Segal-Shale-Weil representation and the geometry of  $\mathrm{Sp}(n, \mathbb{Z}) \backslash \mathrm{Sp}(n, \mathbb{R})$ . (Received September 14, 2020)