Arda H. Demirhan\* (ademir3@uic.edu), 851 S Morgan St (MC 251), University of Illinois at Chicago, Chicago, IL 60607, and Ramin Takloo-Bighash, 851 S Morgan St (MC 251), University of Illinois at Chicago, Chicago, IL 60607. Distribution of Rational Points on Toric

Varieties. Preliminary report.

Manin's conjecture for Fano varieties predicts an asymptotic formula for the number of rational points of bounded height with respect to the anti-canonical height function on a small enough Zariski open set with a dense set of rational points. In the case of toric varieties, Manin's conjecture was verified by Victor Batyrev and Yuri Tschinkel. In this talk, we will explain a multi-height variant of the Batyrev-Tschinkel theorem proposed by Emmanuel Peyre in his paper "Liberté et accumulation" where one considers at height boxes, instead of a single height function, as a way to get rid of accumulating subvarieties. This is our main result: Let X be an arbitrary toric variety over a number field F, and let  $H_i$ ,  $1 \le i \le r$ , be height functions associated to the generators of the cone of effective divisors of X. Fix positive real numbers  $a_i$ ,  $1 \le i \le r$ . Then the number of rational points  $P \in X(F)$  such that for each i,  $H_i(P) \le B^{a_i}$  as B gets large is equal to  $CB^{a_1+\cdots+a_r} + O(B^{a_1+\cdots+a_r-\epsilon})$  for an  $\epsilon > 0$ . Our result is a first example of a large family of varieties along the lines of Peyre's idea. (Received September 14, 2020)