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Carmelo A. Finocchiaro, Sophie Frisch and Daniel Windisch* (dwindisch@math.tugraz.at). Prime Ideals in Infinite Products of Commutative Rings. Preliminary report.

In this talk, we present descriptions of prime ideals and in particular of maximal ideals in products $R = \prod D_{\lambda}$ of families $(D_{\lambda})_{\lambda \in \Lambda}$ of commutative rings. Every maximal ideal is induced by an ultrafilter on the Boolean algebra $\prod \mathcal{P}(\max(D_{\lambda}))$. If every D_{λ} is in a certain class of rings including finite character domains and one-dimensional domains, then this leads to a characterization of the maximal ideals of R. If every D_{λ} is a Prüfer domain, we depict all prime ideals of R. Moreover, we give an example of a (optionally non-local or local) Prüfer domain such that every non-zero prime ideal is of infinite height.

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