We study the generating function associated to complexity sequence of the twisted construction of an $N$-graded ring. We regard this as an object reflecting the properties of the ring and its grading and perform a detailed analysis of the case of the polynomial ring with general $N$-grading. Applications to the Frobenius complexity of determinantal rings are provided. (Received September 13, 2020)