## 1163-30-848 **Timothy J. Ferguson\*** (tjferguson1@ua.edu). Bergman and Szegö projections, Extremal Problems, and Square Functions.

We study estimates for Hardy space norms of analytic projections. We first find a sufficient condition for the Bergman projection of a function in the unit disc to belong to the Hardy space  $H^p$  for 1 . We apply the result to provea converse to an extension of Ryabykh's theorem about Hardy space regularity for Bergman space extremal functions. $We also prove that the <math>H^q$  norm of the Szegö projection of  $F^{p/2}\overline{F}^{(p/2)-1}$  cannot be too small if F is analytic, for certain values of p and q. We apply this to show that the best analytic approximation in  $L^p$  of a function in both  $L^p$  and  $L^q$  will also lie in  $L^q$ , for certain values of p and q. (Received September 13, 2020)