The classical spherical functions on compact symmetric spaces form sets of orthogonal polynomials, which can be identified with subclasses of Jacobi polynomials in the so-called rank 1 case and with Heckman-Opdam polynomials with special values for the parameters for higher rank cases. We discuss a general way for obtaining matrix valued orthogonal polynomials related to compact symmetric spaces under some specific conditions. For the group case corresponding to $S U(n)$, we make this explicit. In this way we find matrix valued polynomial analogs of Koornwinder's 2 -variable polynomials orthogonal on the interior of Steiner's hypocycloid corresponding to $n=3$. (Received September 14, 2020)

