1163-47-182 Kelly Bickel, Anne Greenbaum, Pamela Gorkin\* (pgorkin@bucknell.edu), Thomas Ransford, Felix Schwenninger and Elias Wegert. Crouzeix's Conjecture and Related Problems.

Let W(A) denote the numerical range of an  $n \times n$  matrix A:

$$W(A) = \{ \langle Ax, x \rangle : ||x|| = 1 \}.$$

Michel Crouzeix showed that there is a constant C such that

$$||f(A)|| \le C \sup_{z \in W(A)} |f(z)|,$$

for all f analytic on a neighborhood of W(A) and he conjectured that the best constant is C = 2. In this talk, we present a short history of work on the conjecture, some recent results, and open questions related to this conjecture. (Received August 25, 2020)