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David Boozer* (adboozer@princeton.edu). *Computer Bounds for Kronheimer-Mrowka Foam Evaluation.*

Kronheimer and Mrowka recently suggested a possible approach towards a new proof of the four color theorem that does not rely on computer calculations. Their approach is based on a functor J^\sharp , which they define using gauge theory, from the category of webs and foams to the category of vector spaces over the field of two elements. They also consider a possible combinatorial replacement J^\flat for J^\sharp . Of particular interest is the relationship between the dimension of $J^\flat(K)$ for a web K and the number of Tait colorings $\text{Tait}(K)$ of K ; these two numbers are known to be identical for a special class of “reducible” webs, but whether this is the case for nonreducible webs is not known. We describe a computer program that strongly constrains the possibilities for the dimension and graded dimension of $J^\flat(K)$ for a given web K , in some cases determining these quantities uniquely. We present results for a number of nonreducible example webs. For the dodecahedral web W_1 the number of Tait colorings is $\text{Tait}(W_1) = 60$, but our results suggest that $\dim J^\flat(W_1) = 58$. (Received August 20, 2020)