1163-M5-749 Anil Venkatesh* (avenkatesh@adelphi.edu) and Viren Sachdev. Internal Symmetries in Musical 12-Tone Rows.
In music, a 12 -tone row is any of the 12 ! possible orderings of notes in the Western chromatic scale. The musical notes of a 12 -tone composition must always arise in the same order, cycling repeatedly through a predetermined "row" of twelve notes. The repetitive structure of 12 -tone music lends itself to mathematical study. In 2003, Hunter and von Hippel investigated symmetry in 12-tone rows, using group theory to enumerate equivalence classes of rows under a group of music-theoretic symmetries. They found that highly symmetric rows constitute just $0.13 \%$ of the 12 ! possibilities, and yet these rows arise in $10 \%$ of actual compositions. In a previous talk, we conjectured that the remaining $90 \%$ of 12 -tone compositions, while not entirely self-symmetric, might contain shorter repetitions and symmetries that were intuitively attractive to the composers. In this talk, we introduce a way to measure the occurrence of short repetitions and symmetries that go undetected in the analysis of Hunter and von Hippel. We present a new hierarchy of symmetry for 12 -tone rows and show that composers favor symmetric substructures in their work. (Received September 12, 2020)

