

**Meeting:** 1003, Atlanta, Georgia, SS 24A, AMS Special Session on Design Theory and Graph Theory, I

1003-05-1261      **Curtis Clark\*** ([cuclark@morehouse.edu](mailto:cuclark@morehouse.edu)), Department of Mathematics, Morehouse College, 830 Westview Drive, Atlanta, GA 30314. *On Maximal Ultimately Economical Subgraphs*. Preliminary report.

Let  $F$  be a graph with no isolated vertices and  $q$  edges. The economical  $F$ -achievement game on the complete graph  $K(n)$  is a two-player game. Player A first colors an edge green. Then Player B colors a different edge red. They continue alternately coloring the edges. The graph  $F$  is  $e$ -achievable on  $K(n)$  if Player A can make a copy of  $F$  in his color in  $q$  moves. The graph  $F$  is ultimately economical (u.e.) if there exists a  $t$  such that  $F$  is  $e$ -achievable on  $K(t)$ . If a graph  $F$  is not ultimately economical, then the u.e. minus number of  $F$ ,  $uemn(F)$ , is the least number of edges that must be deleted from  $F$  so that the remaining subgraph is ultimately economical. We determine  $uemn(F)$  for cycles, theta-graphs, and complete bipartite graphs, and some bounds for complete graphs. We show that maximal u.e. subgraphs are not unique, and exhibit graphs  $F$  such that for any nonnegative integer  $r$ ,  $uemn(F) = r$ . (Received October 04, 2004)