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Zoltán Füredi, Robert H. Sloan and Ken Takata*, Dept. of Math. and C.S., Adelphi University, P.O. Box 701, Garden City, NY 11530-0701, and **György Turán**. *Set systems with the minimal number of sets and the $(4,3)$ -threshold property.*

For n , k , and t such that $1 < t < k < n$, a set \mathcal{F} of subsets of $[n]$ has the (k, t) -*threshold property* if every k -subset of $[n]$ contains at least t sets from \mathcal{F} and if every $(k - 1)$ -subset of $[n]$ contains fewer than t sets. The minimal number of sets in a set system with this property is denoted by $m(n, k, t)$, and such a set system is called an *optimal system*. $m(n, 4, 3)$ can be determined *exactly* for n sufficiently large. We will first give an example of an optimal system (called a *packing construction*) that uses only 2-sets and 3-sets. Then we will show how all other optimal systems with the $(4,3)$ -threshold property can be derived from packing constructions and how the number of packing constructions gives an upper bound on the total number of optimal systems. (Received September 27, 2005)