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John W Snow* (jsnow@shsu.edu), Department of Mathematics and Statistics, Sam Houston State University, Huntsville, TX 77341-2206. *M_4 and Congruence Heredity.*

The notions of congruence heredity and power heredity were recently introduced by Palfy and Hegedus. A congruence lattice L of a finite algebra A is hereditary if every 0-1 sublattice of L is the congruence lattice of an algebra with the same universe as A . L is power hereditary if every 0-1 sublattice of L^n is a congruence lattice on the universe of A^n for all n .

The author recently proved that every congruence lattice representation of N_5 is power hereditary. Palfy recently demonstrated a non-power-hereditary representation of M_3 . To date, there is no known hereditary representation of M_4 .

In this talk, we will prove if A is a finite algebra satisfying a nontrivial idempotent Maltsev condition and if the congruence lattice of A contains a copy of M_4 , then the congruence lattice of A is not hereditary. (Received July 18, 2005)