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**Genghun Eng\*** (genghun.eng@aero.org), 5215 Lenore Street, Torrance, CA 90503. *Deriving The Prime Number Theorem (PNT) and Littlewood Oscillations Using a Nonlinear Dynamical Equation Method.* Preliminary report.

Modeling Eratosthenes Sieve with sets of  $\delta$ -functions gives a Prime Density, smoothable into  $\rho_S(N)$ . The fraction of integers not divisible by primes up to  $N$  can be smoothed into  $\rho_D(N)$ . Since primes  $< N$  determine all primes in  $Q = [N^1, N^2]$ , which best gives  $\rho_S(Q) \equiv \rho_D(N)$ ? A general model is  $\rho_S(Q = N^{\Lambda(Q)}) = \rho_D(N)$ . If  $\Lambda(Q) \Rightarrow \Lambda_o$  at large  $Q$ , then  $\rho_D(Q)$  is governed by a nonlinear dynamical equation:

$$\mathbf{1}(d/dQ)\rho_D(Q) + \rho_D(Q)\rho_D(Q^{+1/\Lambda_o})/Q + \text{Order}[1/Q^2] \equiv 0,$$

giving  $\rho_D(Q) = \mathbf{1}/[\Lambda_o \ln(Q)]$  and  $\rho_S(Q) = \mathbf{1}/\ln(Q)$ . Mertens' Theorem sets  $\rho_D(Q) = 1/[\Lambda_F \ln(Q)]$ , with  $\Lambda_F \approx 1.781$ , giving a new elementary PNT proof. Let  $\rho_D(Q) = 1/[\Lambda_o[1 + Z(Q)] \ln(Q)]$  with  $Z(Q) \ll 1$ :

$$(d/dQ)Z(Q) + Z(Q^{+1/\Lambda_o})/[Q \ln(Q)] \approx 0,$$

then  $Z(Q) = \sum A_m/[\ln(Q)]^{+\beta_m}$  with  $\beta_m \equiv \Lambda_o^{+\beta_m}$ . If  $\Lambda_o > e^{(+1/e)} \approx 1.44$ , complex  $\beta_m$  are allowed, deriving Littlewood Oscillations; all nearly periodic in  $[\ln \ln(Q)]$ . For the PNT,  $Z(Q, \Lambda_F)$  is small, with  $\beta_0(\Lambda_F \approx (1.2069 + \mathbf{i}1.6036))$ , and  $\beta_1(\Lambda_F) \approx (4.54656 + \mathbf{i}13.0248)$ . (Received September 29, 2005)