

1014-13-644

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Let R be a Noetherian local ring with infinite residue field k and I an R -ideal. The core of I , $\text{core}(I)$, is defined to be the intersection of all (minimal) reductions of I . Under some technical conditions (which are automatically satisfied in case I is equimultiple) Polini and Ulrich have shown that for a Gorenstein local ring,

$$J^{n+1} : I^n \subset \text{core}(I) \subset J^{n+1} : \sum_{y \in I} (J, y)^n$$

for $n \gg 0$, and J a minimal reduction of I . This holds in any characteristic. They also show that if $\text{char } k = 0$ or $\text{char } k \gg 0$, then $\text{core}(I) = J^{n+1} : I^n = J^{n+1} : \sum_{y \in I} (J, y)^n$ for $n \gg 0$. We present an example where $\text{char } k = 2$ and $\text{core}(I) \neq J^{n+1} : \sum_{y \in I} (J, y)^n$. On the other hand, we show that if R is a positively graded Gorenstein reduced k -algebra (k an infinite perfect field) and I is an R -ideal generated by forms of the same degree then $\text{core}(I) = J^{n+1} : I^n$ in any characteristic. Part of this work is joint with Claudia Polini and Bernd Ulrich. (Received September 22, 2005)