

1014-57-845

David G.C. Handron* (handron@andrew.cmu.edu), Department of Mathematical Sciences, Carnegie Mellon University, Wean Hall 6113, Pittsburgh, PA 15237. *The Euler Characteristic of Graph Configuration Spaces.*

The graph configuration space $C_G(M)$ of a graph G in a manifold M is the space of all functions from the vertex set $V(G)$ into M , $\alpha : V(G) \rightarrow M$, with the restriction that $\alpha(v_1) \neq \alpha(v_2)$ whenever v_1 and v_2 are adjacent in G . There is a natural interpretation of this space as a subspace of the k -fold product $M^{\times k}$, where k is the number of vertices of G .

This paper is devoted to computing the Euler characteristic $\chi(C_G(M))$ of the graph configuration space $C_G(M)$. It is shown that $\chi(C_G(M))$ for any graph G is a polynomial function of $\chi(M)$. The expression is recursive, in that it may be expressed in terms of the Euler characteristics of the contractions of G .

The main tool used in this paper is Morse theory for stratified spaces. A stratified Morse function f is defined on the product $M^{\times k}$ in such a way that $-f$, when restricted to $C_G(M)$, is also a Morse function. A comparison of the critical points of f and $-f|_{C_G(M)}$ yields the desired result. Examples are computed for several families of graphs, including complete graphs, cyclic graphs and path graphs. (Received September 25, 2005)