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**Yong-Geun Oh\*** (oh@math.wisc.edu), Department of Mathematics, University of Wisconsin-Madison, 480 Lincoln Drive, Madison, WI 53706. *Towards the continuous Hamiltonian dynamical systems.*

We first introduce the notion of the  $(C^0)$  *Hamiltonian topology* on the space of Hamiltonian paths, and on the group of Hamiltonian diffeomorphisms respectively. We then define a *group* denoted by  $Hameo(M, \omega)$  consisting of *Hamiltonian homeomorphisms* that we also define. We prove that  $Ham^{(1,1)}(M, \omega) \subsetneq Hameo(M, \omega) \subset Sympeo(M, \omega)$  where  $Sympeo(M, \omega)$  is the group of symplectic homeomorphisms and  $Ham^{(1,1)}(M, \omega)$  is the set of homeomorphisms obtained by the time-one maps of  $C^{(1,1)}$  time-dependent Hamiltonian functions. We prove that  $Hameo(M, \omega)$  is a *normal subgroup* of  $Sympeo(M, \omega)$  which is path-connected and so contained in the identity component  $Sympeo_0(M, \omega)$  of  $Sympeo(M, \omega)$ . In the case of two dimensional compact surfaces, we prove that the *mass flow* of any element from  $Hameo(M, \omega)$  vanishes, which in turn implies that  $Hameo(M, \omega)$  is strictly smaller than the identity component of the group of area preserving homeomorphisms when  $M \neq S^2$ . For the case of  $S^2$ , we conjecture that the same is still true. (The latter group turns out to coincide with  $Sympeo_0(M, \omega)$  for two dimensional surface  $M$ .) (Received September 16, 2005)