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Finite Dimensional Approximations to Wiener Measure on a Compact Manifold with Positive Curvature.

Let $H(M)$ be the Hilbert manifold of finite energy paths into a compact Riemannian manifold, M . We will equip $H(M)$ with its natural G^1 metric. Given a partition, \mathcal{P} of $[0, 1]$, let $H_{\mathcal{P}}(M)$ be the finite dimensional Riemannian submanifold of $H(M)$ consisting of piecewise geodesic paths adapted to \mathcal{P} . Under certain curvature restrictions on M , it is shown that

$$\frac{1}{Z_{\mathcal{P}}} e^{-\frac{1}{2}E(\sigma)} dVol_{H_{\mathcal{P}}}(\sigma) \rightarrow \rho(\sigma) d\nu(\sigma) \text{ as } \text{mesh}(\mathcal{P}) \rightarrow 0,$$

where $Z_{\mathcal{P}}$ is a “normalization” constant, $E : H(M) \rightarrow [0, \infty)$ is the energy functional, $Vol_{H_{\mathcal{P}}}$ is the Riemannian volume measure on $H_{\mathcal{P}}(M)$, ν is Wiener measure on continuous paths on M , and ρ is a certain density determined by the curvature tensor of M . (Received September 26, 2005)