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Steve Butler* (sbutler@math.ucsd.edu), Department of Mathematics, University of California, San Diego, La Jolla, CA 92093-0112. *The Moebius transform of the triangular numbers.*

We give an interpretation for the Moebius transform of the triangular numbers. In particular we will show that if $\mu(n)$ is the Moebius function and T_n is the n th triangular number,

$$|\{(x, y) : 1 \leq x \leq y \leq n, \gcd(x, y, n) = 1\}| = \sum_{d|n} \mu(n/d)T_d.$$

This can be generalized to higher dimensions, and as a simple application we will show that

$$|\{(a_1, \dots, a_k) : 1 \leq a_1 \leq \dots \leq a_k \leq n, \gcd(a_1, \dots, a_k) = 1\}| = \sum_{i \geq 1} M(\lfloor n/i \rfloor) \binom{i+k-2}{k-1},$$

where $M(n)$ is Mertens function with the convention that $M(0) = 0$. (Received September 12, 2006)